

Physics data booklet

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Diploma Programme Physics data booklet

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Mathematical equations

Area of a circle	$A = \pi r^2$, where r is the radius
Circumference of a circle	$C = 2\pi r$, where r is the radius
Surface area of a sphere	$A = 4\pi r^2$, where r is the radius
Volume of a sphere	$V = \frac{4}{3}\pi r^3$, where r is the radius

Fundamental constants

Quantity	Symbol	Approximate value
Acceleration of free fall (Earth's surface)	g	9.81ms^{-2}
Gravitational constant	G	$6.67 \times 10^{-11}\text{Nm}^2\text{kg}^{-2}$
Avogadro's constant	N_A	$6.02 \times 10^{23}\text{mol}^{-1}$
Gas constant	R	$8.31\text{JK}^{-1}\text{mol}^{-1}$
Boltzmann's constant	k_B	$1.38 \times 10^{-23}\text{JK}^{-1}$
Stefan–Boltzmann constant	σ	$5.67 \times 10^{-8}\text{Wm}^{-2}\text{K}^{-4}$
Coulomb constant	k	$8.99 \times 10^9\text{Nm}^2\text{C}^{-2}$
Permittivity of free space	ϵ_0	$8.85 \times 10^{-12}\text{C}^2\text{N}^{-1}\text{m}^{-2}$
Permeability of free space	μ_0	$4\pi \times 10^{-7}\text{TmA}^{-1}$
Speed of light in vacuum	c	$3.00 \times 10^8\text{ms}^{-1}$
Planck's constant	h	$6.63 \times 10^{-34}\text{Js}$
Elementary charge	e	$1.60 \times 10^{-19}\text{C}$
Electron rest mass	m_e	$9.110 \times 10^{-31}\text{kg} = 0.000549\text{u} = 0.511\text{MeVc}^{-2}$
Proton rest mass	m_p	$1.673 \times 10^{-27}\text{kg} = 1.007276\text{u} = 938\text{MeVc}^{-2}$
Neutron rest mass	m_n	$1.675 \times 10^{-27}\text{kg} = 1.008665\text{u} = 940\text{MeVc}^{-2}$
Unified atomic mass unit	u	$1.661 \times 10^{-27}\text{kg} = 931.5\text{MeVc}^{-2}$
Solar constant	S	$1.36 \times 10^3\text{Wm}^{-2}$
Fermi radius	R_0	$1.20 \times 10^{-15}\text{m}$

Metric (SI) multipliers

Prefix	Abbreviation	Value
peta	P	10^{15}
tera	T	10^{12}
giga	G	10^9
mega	M	10^6
kilo	k	10^3
hecto	h	10^2
deca	da	10^1
deci	d	10^{-1}
centi	c	10^{-2}
milli	m	10^{-3}
micro	μ	10^{-6}
nano	n	10^{-9}
pico	p	10^{-12}
femto	f	10^{-15}

Unit conversions

$$1 \text{ radian (rad)} \equiv \frac{180^\circ}{\pi}$$

$$\text{Temperature (K)} = \text{temperature (}^\circ\text{C)} + 273$$

$$1 \text{ light year (ly)} = 9.46 \times 10^{15} \text{ m}$$


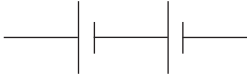

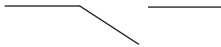

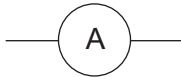

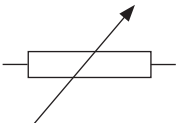


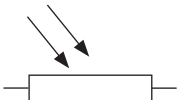
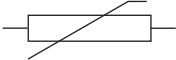
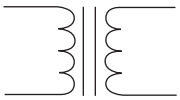
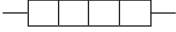
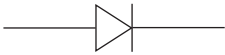

$$1 \text{ parsec (pc)} = 3.26 \text{ ly}$$

$$1 \text{ astronomical unit (AU)} = 1.50 \times 10^{11} \text{ m}$$

$$1 \text{ kilowatt-hour (kWh)} = 3.60 \times 10^6 \text{ J}$$

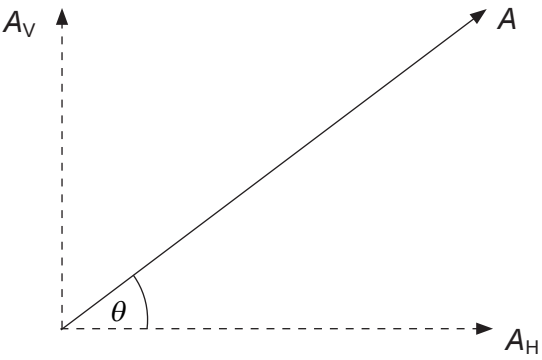
$$hc = 1.99 \times 10^{-25} \text{ Jm} = 1.24 \times 10^{-6} \text{ eVm}$$

Electrical circuit symbols

cell		battery	
ac supply		switch	
voltmeter		ammeter	
resistor		variable resistor	
lamp		potentiometer	
light-dependent resistor (LDR)		thermistor	
transformer		heating element	
diode		capacitor	

Equations—Core

Note: All equations relate to the magnitude of the quantities only. Vector notation has not been used.

Sub-topic 1.2 – Uncertainties and errors	Sub-topic 1.3 – Vectors and scalars
<p>If: $y = a \pm b$ then: $\Delta y = \Delta a + \Delta b$</p> <p>If: $y = \frac{ab}{c}$ then: $\frac{\Delta y}{y} = \frac{\Delta a}{a} + \frac{\Delta b}{b} + \frac{\Delta c}{c}$</p> <p>If: $y = a^n$ then: $\frac{\Delta y}{y} = \left n \frac{\Delta a}{a} \right$</p>	 <p>$A_H = A \cos \theta$</p> <p>$A_V = A \sin \theta$</p>

Sub-topic 2.1 – Motion	Sub-topic 2.2 – Forces
<p>$v = u + at$</p> <p>$s = ut + \frac{1}{2}at^2$</p> <p>$v^2 = u^2 + 2as$</p> <p>$s = \frac{(v + u)t}{2}$</p>	<p>$F = ma$</p> <p>$F_f \leq \mu_s R$</p> <p>$F_f = \mu_d R$</p>
Sub-topic 2.3 – Work, energy and power	Sub-topic 2.4 – Momentum and impulse
<p>$W = F s \cos \theta$</p> <p>$E_k = \frac{1}{2}mv^2$</p> <p>$E_p = \frac{1}{2}k\Delta x^2$</p> <p>$\Delta E_p = mg\Delta h$</p> <p>power = Fv</p> <p>efficiency = $\frac{\text{useful work out}}{\text{total work in}}$ = $\frac{\text{useful power out}}{\text{total power in}}$</p>	<p>$p = mv$</p> <p>$F = \frac{\Delta p}{\Delta t}$</p> <p>$E_k = \frac{p^2}{2m}$</p> <p>impulse = $F\Delta t = \Delta p$</p>

Sub-topic 3.1 – Thermal concepts	Sub-topic 3.2 – Modelling a gas
$Q = mc\Delta T$ $Q = mL$	$p = \frac{F}{A}$ $n = \frac{N}{N_A}$ $pV = nRT$ $\bar{E}_k = \frac{3}{2}k_B T = \frac{3}{2} \frac{R}{N_A} T$

Sub-topic 4.1 – Oscillations	Sub-topic 4.4 – Wave behaviour
$T = \frac{1}{f}$	$\frac{n_1}{n_2} = \frac{\sin \theta_2}{\sin \theta_1} = \frac{v_2}{v_1}$
Sub-topic 4.2 – Travelling waves	$s = \frac{\lambda D}{d}$ Constructive interference: path difference = $n\lambda$ Destructive interference: path difference = $\left(n + \frac{1}{2}\right)\lambda$
$c = f\lambda$	
Sub-topic 4.3 – Wave characteristics	
$I \propto A^2$ $I \propto x^{-2}$ $I = I_0 \cos^2 \theta$	

Sub-topic 5.1 – Electric fields	Sub-topic 5.2 – Heating effect of electric currents
$I = \frac{\Delta q}{\Delta t}$ $F = k \frac{q_1 q_2}{r^2}$ $k = \frac{1}{4\pi\epsilon_0}$ $V = \frac{W}{q}$ $E = \frac{F}{q}$ $I = nAvq$	Kirchoff's circuit laws: $\Sigma V = 0 \text{ (loop)}$ $\Sigma I = 0 \text{ (junction)}$ $R = \frac{V}{I}$ $P = VI = I^2R = \frac{V^2}{R}$ $R_{\text{total}} = R_1 + R_2 + \dots$ $\frac{1}{R_{\text{total}}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$ $\rho = \frac{RA}{L}$
Sub-topic 5.3 – Electric cells	Sub-topic 5.4 – Magnetic effects of electric currents
$\varepsilon = I(R + r)$	$F = qvB \sin \theta$ $F = BIL \sin \theta$
Sub-topic 6.1 – Circular motion	Sub-topic 6.2 – Newton's law of gravitation
$v = \omega r$ $a = \frac{v^2}{r} = \frac{4\pi^2 r}{T^2}$ $F = \frac{mv^2}{r} = m\omega^2 r$	$F = G \frac{Mm}{r^2}$ $g = \frac{F}{m}$ $g = G \frac{M}{r^2}$

Sub-topic 7.1 – Discrete energy and radioactivity	Sub-topic 7.2 – Nuclear reactions
$E = hf$ $\lambda = \frac{hc}{E}$	$\Delta E = \Delta mc^2$

Sub-topic 7.3 – The structure of matter

Charge	Quarks			Baryon number	Charge	Leptons		
$\frac{2}{3}e$	u	c	t	$\frac{1}{3}$	-1	e	μ	τ
$-\frac{1}{3}e$	d	s	b	$\frac{1}{3}$	0	ν_e	ν_μ	ν_τ
All quarks have a strangeness number of 0 except the strange quark that has a strangeness number of -1					All leptons have a lepton number of 1 and antileptons have a lepton number of -1			

	Gravitational	Weak	Electromagnetic	Strong
Particles experiencing	All	Quarks, leptons	Charged	Quarks, gluons
Particles mediating	Graviton	W^+, W^-, Z^0	γ	Gluons

Sub-topic 8.1 – Energy sources	Sub-topic 8.2 – Thermal energy transfer
$\text{power} = \frac{\text{energy}}{\text{time}}$ $\text{power} = \frac{1}{2} A \rho v^3$	$P = e\sigma AT^4$ $\lambda_{\text{max}}(\text{metres}) = \frac{2.90 \times 10^{-3}}{T(\text{kelvin})}$ $I = \frac{\text{power}}{A}$ $\text{albedo} = \frac{\text{total scattered power}}{\text{total incident power}}$

Equations—AHL

Sub-topic 9.1 – Simple harmonic motion	Sub-topic 9.2 – Single-slit diffraction
$\omega = \frac{2\pi}{T}$ $a = -\omega^2 x$ $x = x_0 \sin \omega t; x = x_0 \cos \omega t$ $v = \omega x_0 \cos \omega t; v = -\omega x_0 \sin \omega t$ $v = \pm \omega \sqrt{(x_0^2 - x^2)}$ $E_k = \frac{1}{2} m \omega^2 (x_0^2 - x^2)$ $E_T = \frac{1}{2} m \omega^2 x_0^2$ <p>pendulum: $T = 2\pi \sqrt{\frac{l}{g}}$</p> <p>mass-spring: $T = 2\pi \sqrt{\frac{m}{k}}$</p>	$\theta = \frac{\lambda}{b}$
	Sub-topic 9.3 – Interference
	$n\lambda = d \sin \theta$ <p>Constructive interference: $2dn = \left(m + \frac{1}{2}\right)\lambda$</p> <p>Destructive interference: $2dn = m\lambda$</p>
Sub-topic 9.4 – Resolution	Sub-topic 9.5 – Doppler effect
$\theta = 1.22 \frac{\lambda}{b}$ $R = \frac{\lambda}{\Delta\lambda} = mN$	<p>Moving source: $f' = f \left(\frac{v}{v \pm u_s} \right)$</p> <p>Moving observer: $f' = f \left(\frac{v \pm u_o}{v} \right)$</p> $\frac{\Delta f}{f} = \frac{\Delta \lambda}{\lambda} \approx \frac{v}{c}$

Sub-topic 10.1 – Describing fields	Sub-topic 10.2 – Fields at work	
$W = q\Delta V_e$ $W = m\Delta V_g$	$V_g = -\frac{GM}{r}$	$V_e = \frac{kQ}{r}$
	$g = -\frac{\Delta V_g}{\Delta r}$	$E = -\frac{\Delta V_e}{\Delta r}$
	$E_p = mV_g = -\frac{GMm}{r}$	$E_p = qV_e = \frac{kQq}{r}$
	$F_g = \frac{GMm}{r^2}$	$F_e = \frac{kQq}{r^2}$
	$v_{\text{esc}} = \sqrt{\frac{2GM}{r}}$ $v_{\text{orbit}} = \sqrt{\frac{GM}{r}}$	

Sub-topic 11.1 – Electromagnetic induction	Sub-topic 11.3 – Capacitance
$\Phi = BA \cos \theta$ $\varepsilon = -N \frac{\Delta \Phi}{\Delta t}$ $\varepsilon = Bvl$ $\varepsilon = BvIN$	$C = \frac{q}{V}$ $C_{\text{parallel}} = C_1 + C_2 + \dots$ $\frac{1}{C_{\text{series}}} = \frac{1}{C_1} + \frac{1}{C_2} + \dots$
Sub-topic 11.2 – Power generation and transmission	
$I_{\text{rms}} = \frac{I_0}{\sqrt{2}}$ $V_{\text{rms}} = \frac{V_0}{\sqrt{2}}$ $R = \frac{V_0}{I_0} = \frac{V_{\text{rms}}}{I_{\text{rms}}}$ $P_{\text{max}} = I_0 V_0$ $\bar{P} = \frac{1}{2} I_0 V_0$ $\frac{\varepsilon_p}{\varepsilon_s} = \frac{N_p}{N_s} = \frac{I_s}{I_p}$	$C = \varepsilon \frac{A}{d}$ $E = \frac{1}{2} CV^2$ $\tau = RC$ $q = q_0 e^{-\frac{t}{\tau}}$ $I = I_0 e^{-\frac{t}{\tau}}$ $V = V_0 e^{-\frac{t}{\tau}}$

Sub-topic 12.1 – The interaction of matter with radiation	Sub-topic 12.2 – Nuclear physics
$E = hf$ $E_{\text{max}} = hf - \Phi$ $E = -\frac{13.6}{n^2} \text{eV}$ $mvr = \frac{nh}{2\pi}$ $P(r) = \psi ^2 \Delta V$ $\Delta x \Delta p \geq \frac{h}{4\pi}$ $\Delta E \Delta t \geq \frac{h}{4\pi}$	$R = R_0 A^{\frac{1}{3}}$ $N = N_0 e^{-\lambda t}$ $A = \lambda N_0 e^{-\lambda t}$ $\sin \theta \approx \frac{\lambda}{D}$

Equations—Options

Sub-topic A.1 – The beginnings of relativity	Sub-topic A.2 – Lorentz transformations
$x' = x - vt$ $u' = u - v$	$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$
Sub-topic A.3 – Spacetime diagrams	$x' = \gamma(x - vt); \Delta x' = \gamma(\Delta x - v\Delta t)$
$\theta = \tan^{-1}\left(\frac{v}{c}\right)$	$t' = \gamma\left(t - \frac{vx}{c^2}\right); \Delta t' = \gamma\left(\Delta t - \frac{v\Delta x}{c^2}\right)$ $u' = \frac{u - v}{1 - \frac{uv}{c^2}}$ $\Delta t = \gamma \Delta t_0$ $L = \frac{L_0}{\gamma}$ $(ct')^2 - (x')^2 = (ct)^2 - (x)^2$
Sub-topic A.4 – Relativistic mechanics (HL only)	Sub-topic A.5 – General relativity (HL only)
$E = \gamma m_0 c^2$ $E_0 = m_0 c^2$ $E_k = (\gamma - 1)m_0 c^2$ $p = \gamma m_0 v$ $E^2 = p^2 c^2 + m_0^2 c^4$ $qV = \Delta E_k$	$\frac{\Delta f}{f} = \frac{g\Delta h}{c^2}$ $R_s = \frac{2GM}{c^2}$ $\Delta t = \frac{\Delta t_0}{\sqrt{1 - \frac{R_s}{r}}}$

Sub-topic B.1 – Rigid bodies and rotational dynamics	Sub-topic B.2 – Thermodynamics
$\Gamma = Fr \sin \theta$ $I = \sum mr^2$ $\Gamma = I\alpha$ $\omega = 2\pi f$ $\omega_f = \omega_i + \alpha t$ $\omega_f^2 = \omega_i^2 + 2\alpha\theta$ $\theta = \omega_i t + \frac{1}{2}\alpha t^2$ $L = I\omega$ $E_{K_{\text{rot}}} = \frac{1}{2}I\omega^2$	$Q = \Delta U + W$ $U = \frac{3}{2}nRT$ $\Delta S = \frac{\Delta Q}{T}$ $\rho V^{\frac{5}{3}} = \text{constant (for monatomic gases)}$ $W = p\Delta V$ $\eta = \frac{\text{useful work done}}{\text{energy input}}$ $\eta_{\text{Carnot}} = 1 - \frac{T_{\text{cold}}}{T_{\text{hot}}}$
Sub-topic B.3 – Fluids and fluid dynamics (HL only)	Sub-topic B.4 – Forced vibrations and resonance (HL only)
$B = \rho_f V_f g$ $P = P_0 + \rho_f g d$ $Av = \text{constant}$ $\frac{1}{2}\rho v^2 + \rho g z + p = \text{constant}$ $F_D = 6\pi\eta r v$ $R = \frac{vr\rho}{\eta}$	$Q = 2\pi \frac{\text{energy stored}}{\text{energy dissipated per cycle}}$ $Q = 2\pi \times \text{resonant frequency} \times \frac{\text{energy stored}}{\text{power loss}}$

Sub-topic C.1 – Introduction to imaging	Sub-topic C.2 – Imaging instrumentation
$\frac{1}{f} = \frac{1}{v} + \frac{1}{u}$ $P = \frac{1}{f}$ $m = \frac{h_i}{h_o} = -\frac{v}{u}$ $M = \frac{\theta_i}{\theta_o}$ $M_{\text{near point}} = \frac{D}{f} + 1; M_{\text{infinity}} = \frac{D}{f}$	$M = \frac{f_o}{f_e}$
	Sub-topic C.3 – Fibre optics
	$n = \frac{1}{\sin c}$ $\text{attenuation} = 10 \log \frac{I}{I_0}$
	Sub-topic C.4 – Medical imaging (HL only)
	$L_1 = 10 \log \frac{I_1}{I_0}$ $I = I_0 e^{-\mu x}$ $\mu x_{\frac{1}{2}} = \ln 2$ $Z = \rho c$

Sub-topic D.1 – Stellar quantities	Sub-topic D.2 – Stellar characteristics and stellar evolution
$d(\text{parsec}) = \frac{1}{p(\text{arc-second})}$ $L = \sigma AT^4$ $b = \frac{L}{4\pi d^2}$	$\lambda_{\text{max}} T = 2.9 \times 10^{-3} \text{ mK}$ $L \propto M^{3.5}$
Sub-topic D.3 – Cosmology	Sub-topic D.5 – Further cosmology (HL only)
$z = \frac{\Delta\lambda}{\lambda_0} \approx \frac{v}{c}$ $z = \frac{R}{R_0} - 1$ $v = H_0 d$ $T \approx \frac{1}{H_0}$	$v = \sqrt{\frac{4\pi G \rho}{3}} r$ $\rho_c = \frac{3H^2}{8\pi G}$